Integrating the Standards for Mathematical Practice Into Your Daily Lessons

Part 1 - Standards 1, 2, 3, 6

Dr. Janet Stramel

Hello!

Fort Hays State University

- Mathematics Methods
- Concepts of Elementary Mathematics

National Board Certified Teacher

• Early Adolescence Mathematics

Middle School Mathematics Teacher

I am Dr. Janet Stramel.

I am here because I love teaching mathematics and love to give presentations.

You can find me at jkstramel@fhsu.edu





The Standards for Mathematical Practice reflect what it means to "do mathematics." This session will give you suggestions for incorporating them into your everyday mathematics instruction.

Standards for Mathematical Practice

Mathematically proficient students—

- **explain** to themselves the meaning of a problem and look for entry points to its solution.
- make sense of quantities and their relationships in problem situations.
- use assumptions, definitions, and previously established results in constructing arguments.
- apply the mathematics they know to solve problems arising in everyday life, society, and the workplace.
- **consider** all available tools when solving a mathematical problem.
- **communicate** precisely to others.
- **look** closely to discern a pattern or structure.
- notice if calculations are repeated and look for general methods and shortcuts.

Standards for Mathematical Practice

Mathematically proficient students do not strictly...

- <u>listen</u> while the teacher provides direct instruction for the entire class period.
- **<u>copy</u>** notes word for word from the board.
- <u>memorize</u> procedures for solving problems and duplicate exact replicas for homework and assessments.
- <u>sit</u> quietly throughout the entire lesson with minimal peer interaction.

Derek Pipkorn http://www.nctm.org/Publications/Mathematics-Teaching-in-Middle-School/Blog/What-Makes-a-Mathematically-Proficient-Student_/



HABITS OF MIND OVERARCHING

problems and persevere in Make sense of

ecision ttend

CCSS Mathematical Practices

REASONING AND EXPLAINING

- Reason abstractly and guantitatively
- 3. Construct viable arguments and critique the reasoning of others

MODELING AND USING TOOLS

- 4. Model with mathematics
- Use appropriate tools strategically

SEEING STRUCTURE AND GENERALIZING

- Look for and make use of structure
- 8. Look for and express regularity in repeated reasoning

https://www.mydigitalchalkboard.org/portal/default/Content/Viewer/Content?action=2&scId=306591&sciId=12783

Standards for Mathematical Practice



Standards 1 and 6 "Overarching Habits of Mind"

Make sense of problems and persevere in solving them

SMP



SMP 1 -

Make sense of problems and persevere in solving them.

- Give students tough tasks and let them work through them.
- O Allow wait time for yourself and your students.
- ◎ Work for progress and "aha" moments.
- O The math becomes about the process and not about the one right answer.
- ◎ Lead with questions, but don't pick up a pencil.
- O Have students make headway in the task themselves.

SMP 1 -Make sense of problems and persevere in solving them.

Teachers:

- Provides time for discussion
- Facilitates classroom discourse
- Provides time for students to become "patient" problem solvers

Students:

- Actively engaged
- O DOING mathematics,
 - not just following the steps or procedures
- Discussing with each other
- Making conjectures
- Continually asking, "Does this make sense?"

- SMP 1 Questions to Develop Mathematical Thinking
- O How would you describe the problem in your own words?
- \bigcirc How would you describe what you are trying to find? \bigcirc What do you potico about 2
- What do you notice about...?
- © What information is given in the problem?
- Obscribe what you have already tried. What might you change?

Talk me through the steps you've used to this point.



SMP



SMP 6 -Attend to precision.

- O Push students to use precise and exact language in math.
- Measurements should be exact, numbers should be precise, and explanations must be detailed.
- One change I've made is not allowing the phrase, "I don't get it."
- Students have to explain exactly what they do and do not understand and where their understanding falls apart.

SMP 6 -Attend to precision.

- Elementary students are solving problems and carefully formulating explanations to others.
- O High School students are examining claims and making explicit use of definitions.



SMP 6 -Attend to precision

Students:

https://www.illustrativemathematics.org/practice-standards/6





Valid Equalities?

<u>+</u> «

Subscribe to our Newsletter!

No Tags

Alignments to Content Standards: 1.OA.D.7

Student View

Task

Decide if the equations are true or false. Explain your answer.

a. 2 + 5 = 6b. 3 + 4 = 2 + 5c. 8 = 4 + 4

https://www.illustrativemathematics.org/content-standards/7/NS/A/1/tasks/314





Comparing Freezing Points

Subscribe to our Newsletter!

About Us

 $\star \prec$

No Tags

Alignments to Content Standards: 7.NS.A.1

Student View

Task

Ocean water freezes at about $-2\frac{1}{2}^*C$. Fresh water freezes at 0^*C . Antifreeze, a liquid used in the radiators of cars, freezes at -64^*C .

Imagine that the temperature has dropped to the freezing point for ocean water. How many degrees more must the temperature drop for the antifreeze to turn solid?

SMP 6 - Questions to Develop Mathematical Thinking

- O How did you know your solution was reasonable?
 O Explain how you might show that your solution answers the problem.
- ◎ Is there a more efficient strategy?

O How are you showing the meaning of the quantities?
O How could you test your solution to see if it answers
The problem?

Standards for Mathematical Practice



Standards 2 and 3 "Reasoning and Explaining"

Reason abstractly and quantitatively

SMP



→ Mathematically proficient students make sense of quantities and their relationships in problem situations.

SMP 2 -Reason abstractly and quantitatively

Teachers:

- Provide a range of problems
- Provide problems that require flexibility
- Emphasize quantitative reasoning

Students:

- O Use varied
 - representations
- Decontextualize and contextualize
- Use quantitative reasoning

https://www.illustrativemathematics.org/practice-standards/2

In the barnyard is an assortment of chickens and pigs. Counting heads, I get 13; counting legs I get 46. How many pigs and chickens are there?

https://achievethecore.org/aligned/digging-deeper-into-smp-2reason-abstractly-and-quantitatively/



Jane wants to save \$53 to buy her cousin a birthday present. She also needs \$34 for a new pair of shoes. How much money will Jane need to save for both?

https://achievethecore.org/aligned/digging-deeper-into-smp-2reason-abstractly-and-quantitatively/

There were 24 boys and 20 girls in a chess club last year. This year the number of boys increased by 25% but the number of girls decreased by 10%. Was there an increase or decrease in overall membership? Find the overall percent change in membership of the club.

*Question taken from Illustrative Mathematics

https://achievethecore.org/aligned/digging-deeper-into-smp-2reason-abstractly-and-quantitatively/

A fisherman illegally introduces some fish into a lake, and they quickly propagate. The growth of the population of this new species (within a period of a few years) is modeled by $P(x) = 5b^x$, where x is the time in weeks following the introduction and b is a positive unknown base.

- a) Exactly how many fish did the fisherman release into the lake?
- Find b if you know the lake contains 33 fish after eight weeks. Show step-by-step work.
- c) Instead, now suppose that P(x) = 5b^x and b = 2. What is the weekly percent growth rate in this case? What does this mean in every-day language?

**Question taken from Illustrative Mathematics

SMP 2 - Questions to Develop Mathematical Thinking

- O What do the numbers used in the problem represent?
- ◎ What is the relationship of the quantities?
- What does mean to you? (e.g. symbol, quantity, diagram)

What properties might we use to find a solution?
How did you decide in this task that you needed to use...?

Construct viable arguments and critique the reasoning of others

SMP

3



SMP 3 -Construct viable arguments and critique the reasoning of others

Teachers:

- Provides opportunities for ALL students
- Provides ample time
- Facilitates and guides students
- O Asks useful questions

Students:

 Makes conjectures
 Justifies and defends all conclusions and communicates them to others

How Do You Know That 23 + 2 = 2 + 23?

- What happens to the sum if the order of the addends is changed?
- Can we change the order of the addends and still get 25?

SMP 3 - Questions to Develop Mathematical Thinking

- O How can we be sure that...? / How could you prove that...? Will it still work if...?
- ◎ What were you considering when...?
- ◎ How did you decide to try that strategy?
- O How did you decide what the problem was asking you to find? (What was unknown?)
- Oid you try a method that did not work? Why didn't it work? Would it ever work? Why or why not?

Illustrative Mathematics: Practice Standards

https://www.illustrativemathematics.org/practice-standards



Mathematics Assessment Project

http://map.mathshell.org/stds.php?standardid=1159

← → C O O map.mathshell.org/stds.php?standardid=1159

🔢 Apps ★ Bookmarks 📙 Imported From Firef: 😨 FHSU 鷆 Blackboard 🛞 ilos M KATM Mail 🎽 TK20 FHSU 💪 Google 🐨 CAEP 🧔 Common Core Math 🗅 Habits + Bloom's = 🗅 **Mathematics Assessment Project** COMMON CORE STATE STANDARDS Mathematical Practices for All Grades About News Lessons Tasks Tests PD Modules TRU Framework Standards QD MP1: Make sense of problems and persevere in solving them All Grades Mathematically proficient students start by explaining to themselves the meaning of a problem and looking for entry points to its solution. They analyze givens, constraints, relationships, and goals. They make conjectures about the form and meaning of the solution and plan a ▼ Standards for Mathematical solution pathway rather than simply jumping into a solution attempt. They consider analogous problems, and try special cases and simpler Practice forms of the original problem in order to gain insight into its solution. They monitor and evaluate their progress and change course if MP1 Make sense of problems necessary. Older students might, depending on the context of the problem, transform algebraic expressions or change the viewing window and persevere in solving on their graphing calculator to get the information they need. them Mathematically proficient students can explain correspondences between equations, verbal descriptions, tables, and graphs or draw MP2 Reason abstractly and diagrams of important features and relationships, graph data, and search for regularity or trends. Younger students might rely on using quantitatively concrete objects or pictures to help conceptualize and solve a problem. Mathematically proficient students check their answers to MP3 Construct viable problems using a different method, and they continually ask themselves, "Does this make sense?" They can understand the approaches of others to solving complex problems and identify correspondences between different approaches. arguments and critique the reasoning of others Optimizing Coverage: Security Describing and Defining Triangles Sorting Equations and Identities MP4 Model with mathematics Cameras Finding Areas of Circles Building and Solving Complex MP5 Use appropriate tools Maximizing Profit: Selling Soup Equations Sampling and Estimating: Counting strategically Using Standard Algorithms for Trees Classifying Equations of Parallel and MP6 Attend to precision Number Operations Perpendicular Lines Designing: A Game of Chance MP7 Look for and make use of Finding Factors and Multiples Interpreting Algebraic Expressions Comparing Data Using Statistical structure Interpreting Multiplication and Measures Generating Polynomials from Division Patterns Evaluating Statements About MP8 Look for and express Translating between Fractions. Probability Solving Linear Equations in Two regularity in repeated reasoning Decimals and Percents Variables Analyzing Games of Chance Adding and Subtracting Directed Representing Linear and Estimating Length Using Scientific Numbers Exponential Growth Mathematical Content Notation Sharing Costs Equitably: Traveling to > Translating Between Repeating Representing Quadratic Functions (High School) School Graphically Decimals and Fractions Mathematical Content Modeling Relationships: Car Skid Solving Quadratic Equations Applying Properties of Exponents (Middle School) Marks Representing Trigonometric Comparing Value for Money: Lesson Types Evaluating Statements: Consecutive Baseball Jerseys Functions Sums Representing Functions of Everyday Generalizing Patterns: The Assessment Task Types Interpreting Equations Situations Difference of Two Squares nk to: Formative Assessment Lessons * Representing the Laws of Arithmetic
 Comparing Fuel Consumption: Representing Inequalities ▶ Evaluating Statements About Graphically Buving Cars Defining Lines by Points, Slopes and Provide Representing Polynomials Number Operations Equations

Equations

- Using Proportional Reasoning Designing 3D Products; Candy Cartons
 - Using Space Efficiently: Packing a
 Interpreting Distance-Time Graphs
 Shadows
- Graphically Classifying Solutions to Systems of Modeling Mation: Rolling Cups
 - Deducting Relationships: Floodlight

Other Resources of Note:

- ◎ Kansas FlipBooks
 - http://community.ksde.org/Default.aspx?tabid=5646
- Blog by Bill McCallum
 - <u>http://commoncoretools.me/</u>
- O You Cubed
 - https://www.youcubed.org/
- O Debbie Waggoner
 - http://www.debbiewaggoner.com/math-practice-standards.html
- Inside Mathematics
 - http://www.insidemathematics.org/

Thank You!



Any questions?

You can find me at jkstramel@fhsu.edu



References

- http://www.nctm.org/Publications/Mathematics-Teaching-in-Middle-School/Blog/What-Makes-a-Mathematically-Proficient-Student_/
- https://www.scholastic.com/teachers/blog-posts/meghaneverette/guide-8-mathematical-practice-standards/
- http://thinkmath.edc.org/
- https://www.nwea.org/blog/2017/practice-makes-perfect-usingpractice-standards-increase-classroom-engagement/
- http://map.mathshell.org/stds.php?standardid=1159
- http://commoncoretools.me/wpcontent/uploads/2014/02/Elaborations.pdf
- https://achievethecore.org